

Math 500 – Fall 2001

Homework # 3

- 1) Given a point  $x_0$  in  $X$  show that the map  $f : Y \rightarrow X \times Y$  given by  $f(y) = (x_0, y)$  is continuous.
- 2) Show the subspace  $(a, b)$  of  $\mathbf{R}$  is homeomorphic to  $(0, 1)$ .
- 3) Show the three metrics defined on  $\mathbf{R}^n$  in class all generate the same topology.
- 4) Let  $d$  be a metric on  $X$ . Show  $d : X \times X \rightarrow \mathbf{R}$  is continuous.
- 5) Let  $d$  be a metric on  $X$ . Define  $d'(x, y) = \min\{d(x, y), 1\}$ . Show  $d'$  is a metric and generates the same topology on  $X$ .